Critical stability conditions in skimmed milk crossflow microfiltration: impact on operating modes

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Abstract — There exists a critical ratio (convection towards the membrane/erosion) in crossflow microfiltration, MF, below which there is no marked fouling by colloidal particles and above which performance are altered: sharp increase of fouling, reduced operating time, large decrease in permeability and solute transmission. This paper outlines the impact of the critical ratio on skimmed milk MF processing (separation of casein micelles from the soluble proteins) and gives objective elements (taking into account the critical ratio) for the selection of start-up procedures and stationary modes of operation: controlled transmembrane pressure or permeation flux; “static” or “dynamic” counter-pressure, the latter achieved by circulating the permeate co-current to the retentate to maintain an equal transmembrane pressure profile along the filtering path. Results showed that the controlled transmembrane pressure mode of operation was appropriate for conducting skimmed milk filtration, since it prevented from sharp increase of the hydraulic resistance of fouling and maintained nearly constant performances (permeability, selectivity) over the course of the time. In order to determine the more appropriate counter pressure mode and to predict skimmed milk performances, a four step method was proposed: i) assessment of the critical ratio; ii) selection of the critical flux at the required wall shear stress; iii) determination of the corresponding critical transmembrane pressure in “dynamic” counter-pressure; iv) calculation of the MF performance in “static” mode taking into account the gradient of transmembrane pressure induced by the retentate pressure drop.

hydrodynamics / crossflow microfiltration / operating mode / critical permeation flux / milk

1. INTRODUCTION

Separation and concentration of casein micelles from soluble proteins of skimmed milk can be achieved by crossflow microfiltration, MF, using a 0.1 μm mean pore diameter. During skimmed milk MF the fouling, mainly due to a deposit of casein micelles at the membrane surface, is dependent on a critical permeation flux, J_{crit}, to wall shear stress, \( \tau_w \) ratio [2, 5]. Under this critical ratio the performance (permeability...
and selectivity) are satisfactory: long MF time with slow increase of fouling and high soluble protein transmission. The permeation flux, J governs convective mass transport to the membrane and $\tau_w$ rules the transport by erosion, hydrodynamic diffusion or “lateral migration” of molecules and particles back from the membrane towards the fluid bulk [1, 3, 7]. The critical ratio can be determined in different ways: (i) with “parametric” experiments consisting of gradual increase of J at constant $\tau_w$ [6] (the highest value for which the transmembrane pressure, $\Delta P$ is stable is the critical flux, defined as the flux under which there is no deposition [4]) or of gradual decrease of $\tau_w$ at constant J or $\Delta P$ [2] (the critical ratio is characterised by a sharp increase in the overall hydraulic resistance, R and decrease in protein transmission); (ii) with several experiments performed with constant J and $\tau_w$ over the course of the time [5]: the limit between steady and “unsteady” (sharp increase in the overall hydraulic resistance) runs defined the critical ratio. The knowledge of the critical ratio enables the operator to determine optimal stable filtration operating conditions for high productivity, low processing costs and minimum cleaning requirements.

However the choice of the modes of operation (controlled $\Delta P$ or J, “static” or “dynamic”1 counter-pressure) and the operating parameters ($\Delta P$ or J, $\tau_w$) is generally done without reference to the critical parameter. The aim of this paper is to show the impact of the critical ratio on MF processing and how to take it into account so as to give objective elements for the selection of the most appropriate start-up procedure and stationary mode of operation.

1 The “dynamic” counter-pressure is achieved by circulating the permeate co-current to the retentate to maintain an equal transmembrane pressure profile along the filtering path [8].

2. MATERIALS AND METHODS

2.1. Fluids

Skimmed milk, heat treated at 63 °C for 15 s, was provided by Compagnie Laitière Européenne (Montauban-de-Bretagne, France). It was heated to 50 °C for 30 min before MF experiments and 0.2 g·L$^{-1}$ sodium azide was added to it to prevent any micro-organism development. The cleaning solutions and water used as well as the cleaning procedures were previously described [3].

2.2. Membranes and microfiltration rig

The membranes were multichannel tubular ceramic Kerasep membranes with a 0.1 µm mean pore diameter (7 channels, alumina membrane on an alumina support, Orelis, Miribel, France). Two membranes of different lengths were used: 0.400 or 0.856 m long, inner diameter 4.33 ± 0.05 or 4.35 ± 0.05 10$^{-3}$ m and membrane area 0.037 or 0.081 m$^2$ respectively. The hydraulic resistances of the 2 cleaned membranes were similar: Rm = 1.4 ± 0.2 × 10$^{11}$ m$^{-1}$. Previous experiments have shown that the performance during skimmed milk MF were independent of the length of the membrane (0.400 or 0.856 m) [3].

The MF rig [2] could operate at various concentrations of the feed stream using a feed-and-bleed mode, at controlled either J or $\Delta P$. It was also equipped with the circulation of the permeate co-current to the retentate which allowed the experiments with simultaneous high $\tau_w$ and low $\Delta P$ to be performed.

2.3. Operating procedures

Every experiment was divided into two phases: a “concentration” phase, similar and reproducible (variation of R < 10%) for all the experiments and a “stepwise” phase or “time” phase. The skimmed milk was filtered at 50 °C.

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– The “concentration” phase, already described [2], was conducted at a volume reduction ratio, VRR = 2.0, value chosen according to industrial use. It was conducted with $\tau_w$ (150 Pa), retentate pressure, $P_r$ ($4.0 \times 10^5$ Pa) and constant $J$ (91 L·h$^{-1}$·m$^{-2}$) or $\Delta P$ ($0.1 \times 10^5$ Pa). In both modes of operation (constant $J$ or $\Delta P$) a $\Delta P$ of $0.1 \times 10^5$ Pa corresponded to a mean value of permeation flux of 91 L·h$^{-1}$·m$^{-2}$ during the “concentration” phase. Once VRR reached the value of 2.0, VRR was maintained as constant by running MF in a feed-and-bleed mode of operation. After this phase of about 45 min, the evolution of irreversible adsorption could be considered as negligible.

– The “stepwise” phase consisted of gradual increases of $\Delta P$ (0.0 – $1.0 \times 10^5$ Pa) at constant $\tau_w$, with 15 min duration at each step ($\tau_w = 100$ Pa, $P_r = 4 \times 10^5$ Pa). Points shown in the charts are the average values of $J$ at the steady state during the step.

– The “time” phase consisted of experiments performed in the course of the time ($\tau_w = 100$ Pa, $P_r = 4 \times 10^5$ Pa) at either constant $J$ (ranging from 38 to 76 L·h$^{-1}$·m$^{-2}$) or $\Delta P$ (ranging from $0.07 \times 10^5$ to $0.47 \times 10^5$ Pa).

Three start-up procedures performed at constant $\Delta P$ were tested. The reference was performed without exceeding the set-up value of $0.1 \times 10^5$ Pa, the other 2 exceeded the set-up value with a maximum $\Delta P$ of 0.3 and $0.5 \times 10^5$ Pa for about 200 s.

Some filtration experiments were performed in duplicate with a good reproducibility (< 5% for permeation flux and protein transmission).

2.4. Calculations

2.4.1. Hydraulic resistances of membrane and fouling layers

According to Darcy’s law,

$$J = \frac{\Delta P}{\mu R}$$  (1)

where $\mu$ is the dynamic viscosity (taken as $0.55 \times 10^{-3}$ Pa·s (water) and $0.60 \times 10^{-3}$ Pa·s (milk MF permeate) at $50^\circ$C), $R$ is the overall hydraulic resistance which is broken down to:

$$R = R_m + R_{if} + R_{rf}$$  (2)

$R_{if}$, hydraulic resistance due to irreversible fouling (adsorption, internal pore blocking, etc.) on the membrane surface or in the membrane matrix.

$R_{rf}$, hydraulic resistance due to reversible phenomena (concentration polarization and/or reversible deposit).

$R_m$ and $R_{if}$ were calculated from different $D_P$ values corresponding to pure water permeation fluxes (between 0 and 500 L·h$^{-1}$·m$^{-2}$) before and after the milk MF respectively.

2.4.2. Wall shear stress, $\tau_w$

$\tau_w$, which represents the forces applied by the fluid flowing tangentially to the membrane on an element of membrane area, was experimentally determined according to:

$$\tau_w = \frac{d \Delta P L}{4 L}$$  (3)

where $L$, the length of the tubular membrane. The pressure drop along the filtering path, $\Delta P_L$, that should be used is that due to the flow through the filter tube. Bernouilli’s equation was then used to calculate the longitudinal pressure drop along the membrane tube once the pressure losses due to recirculation of flow before and after the filter was removed from the measured value of pressure drop. For the experiments, $d$ was taken equal to the initial diameter of the clean membrane. Due to the small variation of $d$ over the course of the time during these experiments ($\Delta d < 3\%$), $\tau_w$ was considered as constant and is given with a 7% error.

The efficient wall shear stress, $\tau_{w\text{eff}}$ was defined as:

$$\tau_{w\text{eff}} = \tau_w - \tau_{w\text{c0}}$$  (4)
with \( \tau_{w0} \), the critical erosion shear stress, under which, at \( J = 0 \text{ L.h}^{-1}.m^{-2} \), there is no transport of particles away from the deposit. \( \tau_{w0} \) depends on the membrane and the solution to be filtered.

### 2.4.3. Selectivity

Transmission, \( Tr \) was calculated as follows:

\[
Tr = \frac{C_p}{C_r}
\]

with \( C_p \), concentration of the component at the outlet of the membrane pores and \( C_r \), concentration of the component in the retentate. \( C_p \) was calculated from the concentration of two samples withdrawn at the outlet of the permeate compartment at \( t \) and \( t + \Delta t \) respectively. The calculation of \( C_p \) (at \( t + 1/2\Delta t \)) was then performed considering the permeate compartment to be a perfectly stirred compartment.

### 2.5. Analyses

Skimmed milk, permeate and retentate samples withdrawn during MF were analysed for \( \alpha \)-lactalbumin (\( \alpha \)-LA) and \( \beta \)-lactoglobulin (\( \beta \)-LG) contents (error = 2%) by reverse phase high pressure liquid chromatography [2]. The turbidity (Turbidimeter, Hach, Namur, Belgium) of the permeate (error = 5%) characterised the transmission of the casein micelles through the membrane. Density (error = 0.2%) was determined using a density meter (DMA 48, AP PAAR, Austria), and the dynamic viscosity of fluids (error = 1%) using a microviscosimeter (D8, Haake, Karsruhe, Germany).

### 3. RESULTS AND DISCUSSION

#### 3.1. Performance of skimmed milk MF

As previously described [5], the performance of the skimmed milk MF is mainly ruled by a deposit composed of retained casein micelles, micro-organisms and soluble proteins at the membrane surface. \( \Delta P \), \( J \) and \( \tau_{w0} \) have been shown to play a major part in MF performance critical zone: when the balance between the convective forces (\( J \)) and crossflow (\( \tau_{w0} \)) is tipped even slightly \( (J/\tau_{w0} > (J/\tau_{w0})_{\text{crit}}) \), the deposit becomes more and more consolidated and irreversible due to its compression under high \( \Delta P \) (that leads to increases in R and soluble protein retention) [2]. Le Berre and Daufin [5] showed that during skimmed milk MF the higher VRR the lower \( J \)crit. The insertion of VRR (effect of protein concentration) in the critical ratio was proposed \( (J/VRR/\tau_{w0}) \) but this result remains to be confirmed not only with 2 VRR values as done previously [5] but by using a large range of VRR.

The performance of skimmed milk MF were characterised using “stepwise” experiments [4] and “time” experiments, all of them performed with “dynamic” counter-pressure mode of operation. Whatever the methodology, the critical zone [2] and the performances (permeability, selectivity) were similar (Fig. 1). Figure 1 shows the performance obtained, for one “stepwise” experiment \( J = f (\Delta P) \), one constant \( J \) “time” experiment, and 4 constant \( \Delta P \) “time” experiments. The evolution of the performance versus \( \Delta P \) showed 3 main steps: when \( \Delta P < 0.15 \times 10^5 \text{ Pa} \), \( J = f (\Delta P) \) was linear and the protein transmissions were high and relatively stable \( (Tr_{\alpha-LA} = 1.00 - 0.90; Tr_{\beta-LG} = 0.90 - 0.80) \); the evolution of \( Tr_{\alpha-LA} \) versus \( \Delta P \) (not shown) was analogous to \( Tr_{\beta-LG} \) evolution (Fig. 1b). Over \( \Delta P = \Delta P_{\text{lim}} = 0.2 \times 10^5 \text{ Pa} \), \( J \) stabilised at a limiting permeation flux, \( J_{\text{lim}} \) of about 76 L-h\(^{-1}\).m\(^{-2}\), and protein transmissions decreased sharply (\( Tr_{\alpha-LA} \) from 0.90 to 0.67; \( Tr_{\beta-LG} \) from 0.80 to 0.55). In the transition zone between 0.15 \times 10^5 \text{ Pa} and \( \Delta P_{\text{lim}} \) an increase in the thickness of the casein micelles deposit occurs [2] and therefore delimited \( J \)crit, defined as the flux under which there is no deposition. \( J \)crit was in the range 65 to 76 L-h\(^{-1}\).m\(^{-2}\) (Fig. 1a). A more precise value
3.2. Impact of the critical ratio on the selection of the operating mode

3.2.1. Constant J and ΔP modes of operation

Under the critical ratio \((J/\tau_{w,0})_{\text{crit}} = 0.95 \text{ L.h}^{-1}\text{m}^{-2}\text{Pa}^{-1}; \tau_{w,0} = 18 \text{ Pa}\) similar performances were observed whatever the operating modes (J or ΔP constant) in “time” experiments performed with “dynamic” mode: at constant \(\tau_w = 100 \text{ Pa}\) and \(J = 38 \text{ L.h}^{-1}\text{m}^{-2}\) or \(\Delta P = 0.07 \times 10^5 \text{ Pa}\) the normalised hydraulic resistance, \(R/R_m\), was stable and equal to 7.5, \(T_{r,\alpha,LA} = 0.95\) and \(T_{r,\beta,\LG} = 0.83\) for 4 h.

In order to characterise skimmed milk MF, one 2 h “stepwise” experiment appeared to be less time consuming than “time” experiments: 3 or 4 two hour “time” experiments were actually needed to get to the same information. The former methodology deserves consequently to be preferentially used for the characterisation of a system.

of \(J_{\text{crit}} (72 \pm 2 \text{ L.h}^{-1}\text{m}^{-2})\) could be determined using “parametric” experiments \(\Delta P = f (\tau_w)\) at constant \(J\) or \(\Delta P = f (J)\) at constant \(\tau_w\) \(^2\). When operating at constant \(\tau_w\) (\(\tau_w = 100 \text{ Pa}\) in this work), \(J_{\text{crit}}\) does become the appropriate criterion which must not be exceeded during the process in order to maintain high separation performance.

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Over the critical ratio MF performance depended on the mode of operation:

– at constant \(J\) a sharp increase in \(R/R_m\) (Fig. 2a) and decrease in soluble protein transmission (Fig. 2b) were observed in contrast with constant \(\Delta P\) mode of operation.

– at constant \(\Delta P\) over \(\Delta P_{\text{crit}}\) (= \(0.18 \times 10^5\) Pa, value required to get to \(J_{\text{crit}}\) (Fig. 1a)), the performance were constant over the course of the time: \(J\) was equal to \(J_{\text{lim}}\), that is to say the highest permeation flux that could be achieved under these operating conditions, and the permeate turbidity (which characterised the casein micelles retention) (35 NTU) and soluble protein transmission were constant over the course of the time. Increasing \(\Delta P\) led to stationary \(J = J_{\text{lim}}\) and lower permeate turbidity but higher irreversible and protein transmissions (Fig. 1b) indicating irreversible compression of the deposit formed at the membrane surface.

Thus operating at constant \(\Delta P\) prevented from sharp decrease in MF performance (permeability, selectivity) over the course of an experiment. Moreover, it is not worth working with higher \(\Delta P\), since it would result in increased protein retention and cleaning difficulties. The operating optimum of \(\Delta P\) was found to be \(\Delta P_{\text{crit}}\), needed to get to \(J_{\text{crit}}\), which is close to \(J_{\text{lim}}\) (Fig. 1a). With \(\tau_w\) = 100 Pa and \(\Delta P\) around \(0.18 \times 10^5\) Pa MF performance reached a maximum in permeability for solvent (\(J = 76\) L.h\(^{-2}\).m\(^{-2}\)) and soluble proteins (\(T_{\alpha\text{-LA}} = 0.95; T_{\beta\text{-LG}} = 0.83\)). The determination of \(J_{\text{crit}}\) (and thus \(\Delta P_{\text{crit}}\)) and variations of protein transmission of the system

![Figure 2](image_url)
using “stepwise” experiment were thus essential for the determination of optimal performances.

One can notice that in an industrial use operating at constant flux may be appropriate due to easiness to control especially when ΔPcrit is very low (a few thousands of Pa) as it is the case in skimmed milk MF. Jcrit must therefore not be exceeded in order to avoid sharp increase of fouling and short filtration duration.

3.2.2. Start-up procedure

With the 3 different start-up procedures performed using “dynamic” counter-pressure and constant ΔP modes of operation the higher the exceeding of ΔP (referred to ΔPcrit = 0.18 × 10⁵ Pa), the higher the fouling (R/Rm = 7.0 for no exceeding and 7.8 for a maximum ΔP of 0.5 × 10⁵ Pa after 1 h of filtration) and the lower the protein transmission (Trα-LA = 0.99 and Trβ-LG = 0.85 for no exceeding and Trα-LA = 0.92 and Trβ-LG = 0.83 for a maximum ΔP of 0.5 × 10⁵ Pa). Exceeding ΔPcrit (= 0.18 × 10⁵ Pa) accompanied by transient J values above Jcrit resulted in the formation of an irreversible deposit at the membrane surface. The higher the exceeding the ΔP, the higher the compression of the deposit and the lower the filtration performance. The exceeding for 200 s was however short and performance very close to each other. Further experiments with longer exceedings of the ΔP set-up value need therefore to be performed to confirm these trends and assess the robustness of the MF operation under severe variations of ΔP control.

3.2.3. “Static” and “dynamic” counter-pressure modes of operation

According to the selected mean ΔP significant or no significant differences in performances (always stable over the course of the filtration) could be observed between the 2 counter-pressure modes of operation.

At constant ΔP = 0.19 × 10⁵ Pa, close to ΔPcrit, the “dynamic” counter-pressure led to better performance than the “static” mode: higher J and higher protein transmissions (Tab. I). At a higher ΔP = 0.47 × 10⁵ Pa, far over ΔPcrit, “static” and “dynamic” modes led to similar J (J = Jlim = 76 L·h⁻¹·m⁻²) but lower protein transmissions were obtained in “dynamic” mode (Tab. I).

The results obtained in “static” mode could have been interpreted and predicted from the evolution of the performance (permeability, selectivity) versus ΔP obtained in “dynamic” mode (Fig. 3). From the retentate pressure drop along the membrane in the retentate side, ΔP ≤ ΔPcrit (= 0.18 × 10⁵ Pa) accompanied by transient J values above Jcrit resulted in the formation of an irreversible deposit at the membrane surface. The higher the exceeding the ΔP, the higher the compression of the deposit and the lower the filtration performance. The exceeding for 200 s was however short and performance very close to each other. Further experiments with longer exceedings of the ΔP set-up value need therefore to be performed to confirm these trends and assess the robustness of the MF operation under severe variations of ΔP control.

Table I. Comparison between experimental (Exp) and calculated (Calc) values of permeation flux (J), transmission of β-lactoglobulin (Trβ-LG) and α-lactalbumin (Trα-LA), in “static” and “dynamic” counter-pressure modes of operation.

<table>
<thead>
<tr>
<th></th>
<th>ΔP = 0.19 × 10⁵ Pa</th>
<th>ΔP = 0.47 × 10⁵ Pa</th>
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<tbody>
<tr>
<td></td>
<td>J L·h⁻¹·m⁻²</td>
<td>Trβ-LG</td>
</tr>
<tr>
<td>“dynamic” Exp</td>
<td>76</td>
<td>0.82</td>
</tr>
<tr>
<td>“static” Exp</td>
<td>55</td>
<td>0.74</td>
</tr>
<tr>
<td>“static” Calc</td>
<td>53</td>
<td>0.77</td>
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<tr>
<td>“static” (Exp – Calc) / Exp (%)</td>
<td>4</td>
<td>4</td>
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Experimental conditions: see text.
long membrane) one can determine \( \Delta P \) in any area of the membrane from Figure 3. By integrating the evolution of performance (\( J \) (Fig. 3a) and protein transmissions (Fig. 3b)) along the filtering path (calculation of the area under the experimental curves obtained in “dynamic” mode (Fig. 3)), the expected average performance in “static” mode could be calculated from data obtained in “dynamic” mode (Fig. 3). The calculated and experimental values obtained in “static” mode were in fairly good agreement (< 6%) (Tab. I, Fig. 3). At constant \( \Delta P = 0.19 \times 10^5 \) Pa performance obtained in “static” mode were worse than performance obtained in “dynamic”: in “static” mode the membrane operated partially at low \( \Delta P \) corresponding to \( J < J_{\text{lim}} \) and partially at high \( \Delta P \) corresponding to lower protein transmission. At a higher \( \Delta P = 0.47 \times 10^5 \) Pa the membrane operated totally at a constant \( J = J_{\text{lim}} \) both in “static” and “dynamic” modes, but better protein transmissions in “static” than in “dynamic” mode were predicted due to the non-linearity of protein transmission versus \( \Delta P \) (Fig. 3).

According to these results obtained with \( \tau_w \) as high as 100 Pa the “dynamic” counter-pressure mode must be used at a \( \Delta P \) slightly smaller than \( \Delta P_{\text{crit}} \) for maximum protein transmission. In “static” mode, the large pressure drop along the filtering path, \( \Delta P_L = 0.38 \times 10^5 \) Pa to be compared to \( \Delta P_{\text{crit}} = 0.18 \times 10^5 \) Pa did not make it possible to work in optimal conditions for every area of the filtering path. Selecting a mean \( \Delta P \) significantly lower than \( \Delta P_{\text{crit}} \) (for example
Microfiltration stability and operating modes

The membrane geometry and fluid rheology (VRR, diafiltration rate, etc.) which both affect the retentate pressure drop along the filtering path. The analysis will be completed by taking into account the investment and processing costs.

4. CONCLUSION

For a system mainly ruled by a deposit of retained “species”, the determination of the critical ratio \( J/\tau_{\text{w eff}} \) crit can be done easily using “parametric” studies. The determination of this ratio and of the global performance of the system (permeability and selectivity) versus permeation flux \( J \), transmembrane pressure \( \Delta P \) and wall shear stress, \( \tau_w \) (in “dynamic mode”) enable the optimal stable operating conditions and best modes of operation to be determined. The constant \( \Delta P \) mode is well appropriate (compared to constant \( J \) mode) for conducting filtration runs since it prevents from sharp decrease of performance, which occurs when \( J_{\text{crit}} \) is tipped even slightly over the course of the time. The appropriate value of \( \Delta P \) corresponding to the value of \( J_{\text{crit}} \), close to \( J_{\text{lim}} \), must be used and not exceeded even during the start-up procedures. The better understanding of the performances of a system versus \( \Delta P \) enables the appropriate counter-pressure mode of operation either “static” or “dynamic” to be predicted. The basic principles one can use to determine the more appropriate counter-pressure mode with regard to the operation performance to be achieved are given in that paper. The analysis of the limits and advantages of both modes of operation are to be completed taking into account the investment and processing costs.

REFERENCES


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**List of Symbols**

- $C_p$: permeate concentration (g·L$^{-1}$)
- $C_r$: retentate concentration (g·L$^{-1}$)
- $d$: inner diameter of the membrane (m)
- $J$: permeation flux (m·s$^{-1}$ or L·h$^{-1}$·m$^{-2}$)
- $J_{crit}$: critical permeation flux under which there is no deposition (m·s$^{-1}$ or L·h$^{-1}$·m$^{-2}$)
- $L$: length of the membrane tube (m)
- $P_r$: retentate pressure (Pa or bar)
- $R$: overall hydraulic resistance (m$^{-1}$)
- $R_{if}$: irreversible fouling hydraulic resistance (m$^{-1}$)
- $R_m$: cleaned membrane hydraulic resistance (m$^{-1}$)
- $R_{rf}$: reversible fouling hydraulic resistance (m$^{-1}$)
- $T$: temperature (°C)
- $T_r$: transmission (–)
- $VRR$: volume reduction ratio (–)
- $\alpha$-LA: $\alpha$-lactalbumin
- $\beta$-LG: $\beta$-lactoglobulin
- $\Delta P$: transmembrane pressure (Pa or bar)
- $\Delta P_{crit}$: critical transmembrane pressure, required to get to $J_{crit}$ (Pa or bar)
- $\Delta P_L$: pressure drop along the membrane (Pa or bar)
- $\mu$: dynamic viscosity of the retentate (Pa·s)
- $\tau_w$: shear stress at the membrane wall (Pa)
- $\tau_{wc0}$: critical shear stress at the membrane wall at $J = 0$ L·h$^{-1}$·m$^{-2}$ (Pa)
- $\tau_{w_{eff}}$: efficient shear stress at the membrane wall: $\tau_{w_{eff}} = \tau_w - \tau_{wc0}$ (Pa)